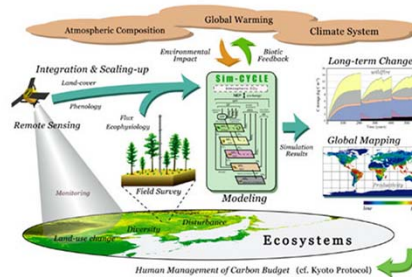


Ecosystem Modeling

- Rationale
- Concepts
 - Hierarchy
 - Components
- History
- General Features
- Performance



Dennis Baldocchi
ESPM
UC Berkeley

4/16/2014

ESPM 111 Ecosystem Ecology

Ecosystem Modeling is an important tool for digesting data, making predictions and to interpolate and extrapolate in time and space.

While this lecture will focus on Ecosystem models per se, so far through this class you have been slowly exposed to a variety of models. Here we pull the ideas together

Why Model Ecosystems?

- Diagnose and Understand Complex sets of Measurements
 - Tease apart convoluted and confounding processes and attributes
 - Provides Paradigm or Hypothesis on how Ecosystem Functions
- Assess behavior in situations and/or at scales or conditions beyond which measurements can be made
 - Regional and Global Scales
 - Reconstruction with Past Climate Data
 - Elevated CO₂, Acid Deposition, Droughts, Warming, Fertilization
 - Long-Term Successional Sequences
- Integrate Information across time and space
 - Interpolate and Extrapolate information
- Predict future conditions and states
- Make Management and Policy Decisions
 - What If Exercises
 - Logging, Gap Size, Fire, Species Removal/Addition, Rate of Spread or Retreat

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All models are wrong; some models are useful

Attributed to George Box, statistician

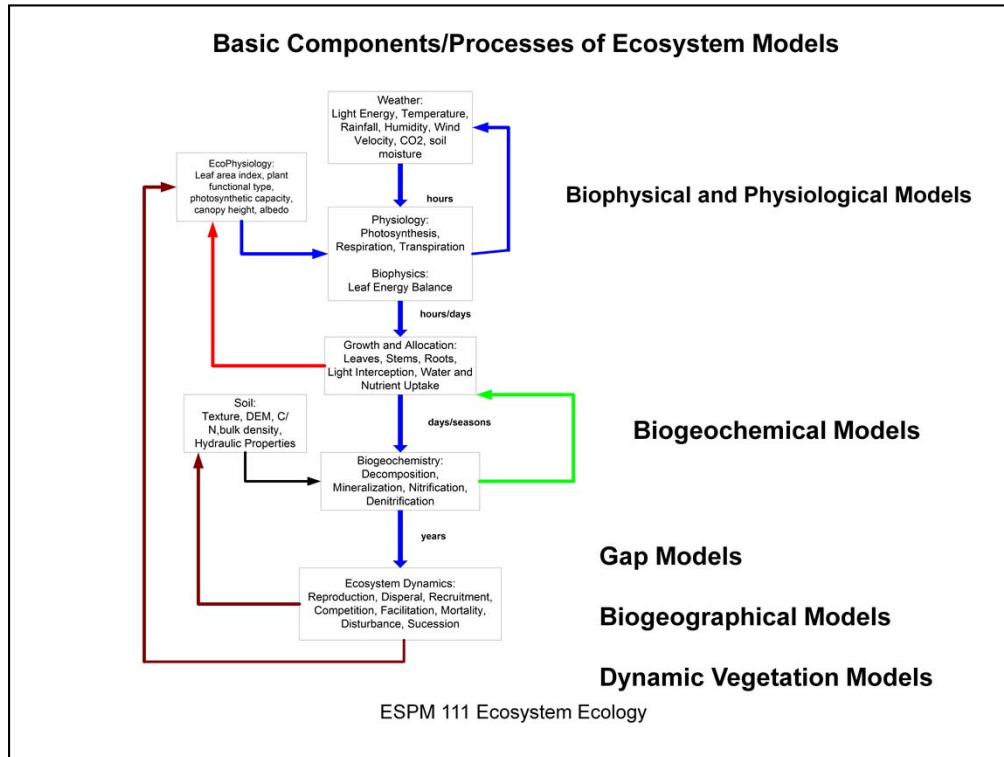


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Since all models are wrong the scientist cannot obtain a "correct" one by excessive elaboration. On the contrary following William of Occam, we should seek an economical description of natural phenomena. Just as the ability to devise simple but evocative models is the signature of the great scientist, so is over-elaboration and over-parameterization often the mark of mediocrity.

This quotation by Box has re-calibrated my perspective on the value of different types of models. I see value in simple toy models, with a few equations and interactions, to tease out some basic understanding of a system. There is merit in simple statistical models for management decisions and there is need for highly mechanistic and theoretical models for prediction and fuller understanding. The type of model you chose and use depends upon you application and the data in hand.

George E. P. Box (1976) [*Science and Statistics*](#) *Journal of the American Statistical Association*, Vol. 71, No. 356. (Dec., 1976), pp. 791-799



As shown early in the semester, this is the conceptual ecosystem ‘model’ we have been dealing with throughout the semester. This is coupled, nested and includes a variety of model classes, including biophysical and physiological models, biogeochemical models, gap, biogeographical and vegetation dynamic models

Set of Ecosystem Topics that are Modeled to different degrees of detail

- Light
- Water
- Carbon Pools
- Nutrients (N, P)
- Climate Interactions (Warming, CO₂)
- Disturbance (Fire, Logging, Grazing)
- Land Use Change
- Pollution and Acid Deposition

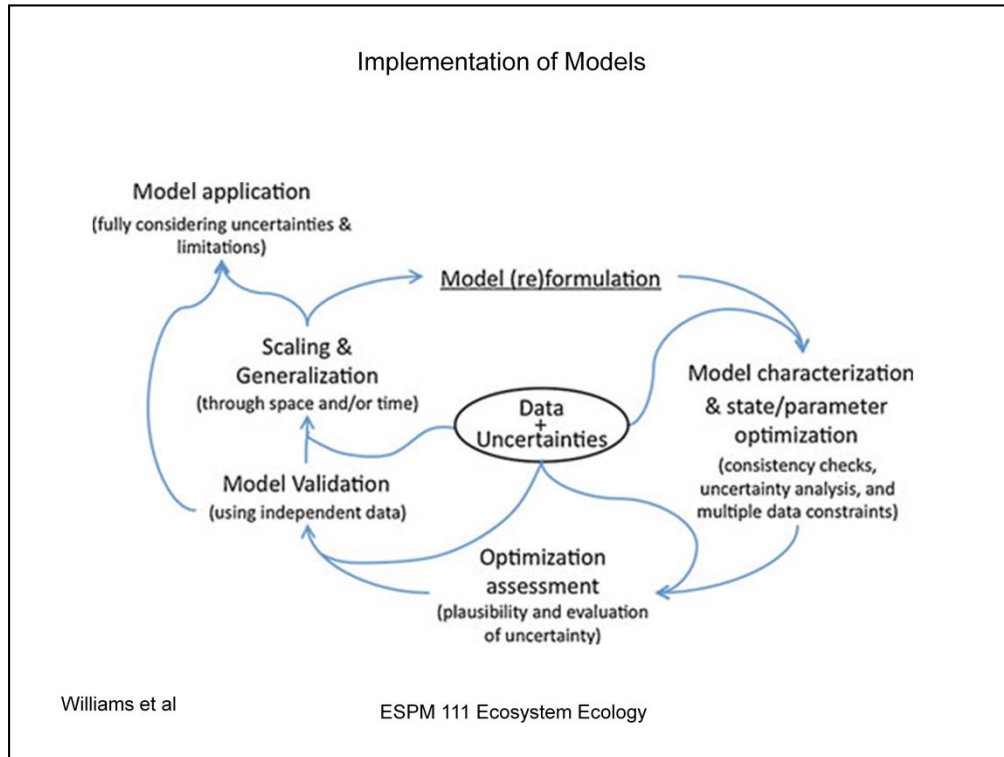
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Different types of ecosystem models serve different purposes. Here is a list of the type of processes these models can address

Sources of Model Uncertainty

- System Complexity
 - Appropriate Set of Equations Must be Applied
- Model Parameters
- Driving Input Variables
- Temporal and Spatial Resolution
 - Time Step, Pixel Resolution, Number of Layers
- Validation Data

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Modeling is an iterative process, balanced by data, experimentation and hypothesis testing. Models tend to represent a 'best' view of a system given current knowledge. But as model algorithms become falsified, we acquire more data and the models and their parameters evolve and improve, new knowledge is achieved.

There remains debate on the merits and demerits of model data fusion, using Bayesian statistics, in this era of big data vs mechanistic models. If there are big datasets to mine and the questions remain within the domain of the dataset, model data fusion has strengths. How well they can predict future states outside the bounds of the data remain contentious. Here is where mechanistic models may have an advantage.

Art of Modeling

- Use Model Hierarchy Assessments to address 'how good is good enough' regarding model detail
- Use Multiple constraints to Minimize over fitting
- Use Independent Data to Fit and to Validate Models
- Consider Representativeness of Data
- Use Good Numeric Methods

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Model Pitfalls

- Garbage In = Garbage Out
- Watch out for Non-Linearities
 - Apply at Proper Time-Step and Space-Scale
- Validate, Validate, Validate
- Don't Parameterize Model Algorithms with the Same data used to Validate
- Equifinality, a combination of parameters yield the same answer
 - An appeal to Multiple Constraints
- Closure: Equal number of Equations and Unknowns is needed
- Avoid Auto-Correlation, $y = f(y)$
- Avoid Extrapolating Empirical Regression models beyond the range of the dataset
- Use Mechanistic and Prognostic Models to predict the future and to upscale information
- Are Driving Variables Representative of the Conditions Experienced by the Organ or Organism?



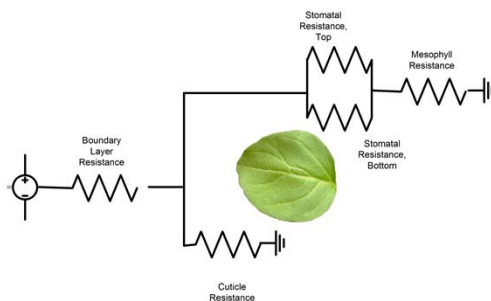
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My experience over the years of some model pitfalls, as well and ideas from a great paper by Belinda Medlyn et al. in Tree Physiology

Biophysical-Physiological Models Based on Ohm's Law and Beer's Law

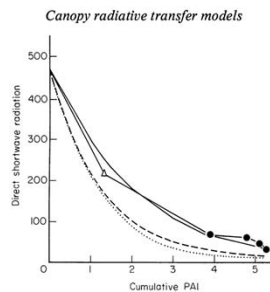
Energy Balance
Water Balance
Photosynthesis
Stomatal Conductance

Light Transmission
Reflectance
Leaf Area Index



$$F = \frac{\Delta V}{\sum R}$$

Leaf Resistance Network



$$I(L) = I(0) \exp(-kL)$$

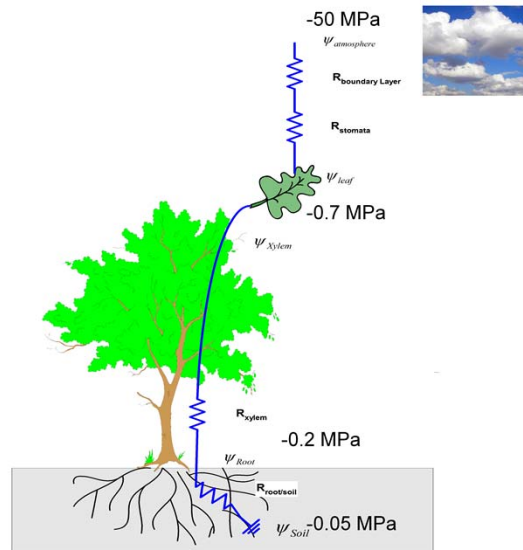
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Ohm's Law is often applied to compute fluxes between leaves/canopies and the atmosphere

Beer's law is important for telling us how much sunlight is available at different locations in the plant canopy. We need to combine Beer's Law and Ohm's law to upscale flux information from the leaf to the canopy

Soil-Plant-Atmosphere-Water Continuum



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Resistance Analog model for water transport through the soil-plant-atmosphere continuum

Mathematical Representation: Model Algorithms

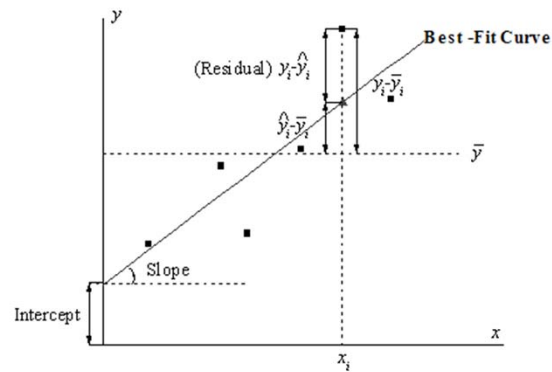
- | | |
|--------------------------------|--|
| 1. Empirical, Regression Based | $f(t, x, y) = af(t) \cdot bf(x) \cdot cf(y)$ |
| 1. Multiplicative | $f(t, x, y) = af(t) + bf(x) + cf(y)$ |
| 2. Additive | $Rn = H + \lambda E + G$ |
| 2. Mechanistic/Diagnostic | |
| 3. Prognostic | $\frac{dc}{dt} = f(c, t)$ |

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Models can be very simple

Minimize the Sum of the Squares

$$\sum (y_i - \hat{y}_i)^2 = \sum (y_i - \beta_0 + \beta_1 x_i)^2$$



$$y = \beta_0 + \beta_1 x$$

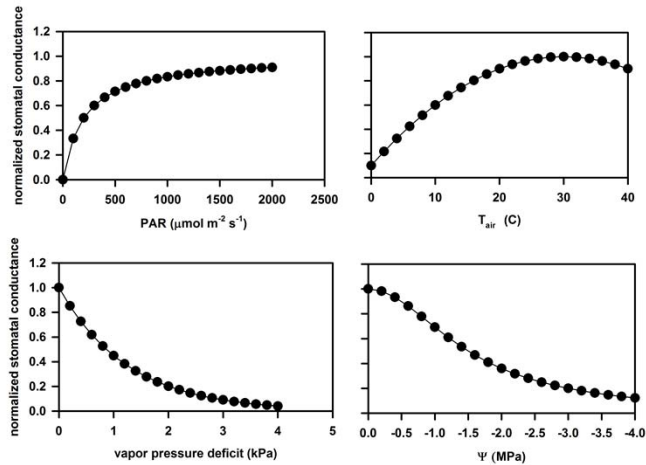
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Least squares fit models, be they linear, non-linear, and multi-variate, are ways of fitting data to simple equations

http://www.originlab.com/www/helponline/origin/en/UserGuide/Illustration_of_the_Least_Squares_Method.html

Multiplicative Model

$$g_s(PAR, VPD, T, \psi) = g_{s, \max} \cdot f_1(PAR) \cdot f_2(VPD) \cdot f_3(T) \cdot f_4(\psi)$$



Concepts of Jarvis Model for Stomatal Conductance

ESPM 129 Biometeorology

Example of Boundary Line Analysis To fit the Jarvis-Reed Model

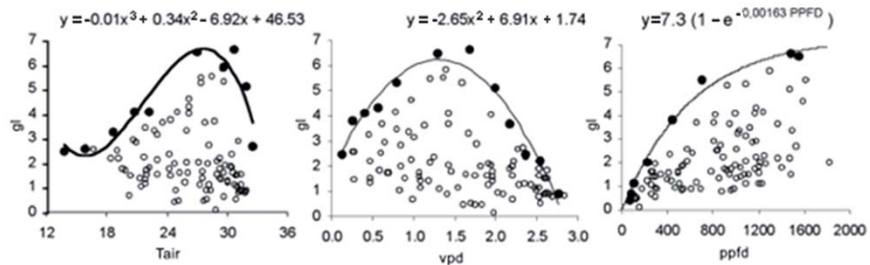


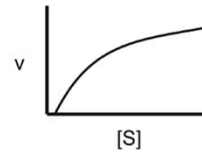
Figure 4. Scatter diagrams of the measurements of leaf diffusive conductance plotted against air temperature, air vapor pressure deficit and photosynthetic photon flux density, with the hypothetical boundary line fitted for each environmental variable.

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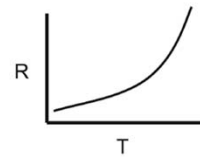
<http://dx.doi.org/10.1590/S1677-04202004000100008>

Non-Linear Biophysical Processes

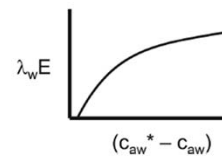
$$v = \frac{V_{\max} [S]}{K_m + [S]}$$



$$R = R_0 e^{(\ln Q_{10}/10) \Delta T}$$



$$\lambda_w E = \frac{s(R_n - G) + \rho_a c_p (c_{aw}^* - c_{aw}) / r_H}{s + \gamma \frac{r_v}{r_H}}$$



Monson and Baldocchi, 2014

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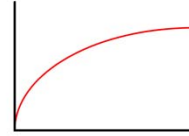
Examples of other models we commonly use to calculate processes like enzyme kinetics, respiration and latent heat of evaporation

Other Non-Linear Biophysical Processes

Photosynthesis

$$A \sim \frac{aI}{b+cI}; \frac{dC}{e+fC}$$

$$aA^3 + bA^2 + cA + d = 0$$



Transpiration

$$e_s(T) \sim \exp(T)$$

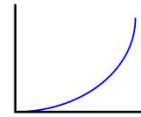
$$aLE^2 + bLE + c = 0$$

Respiration

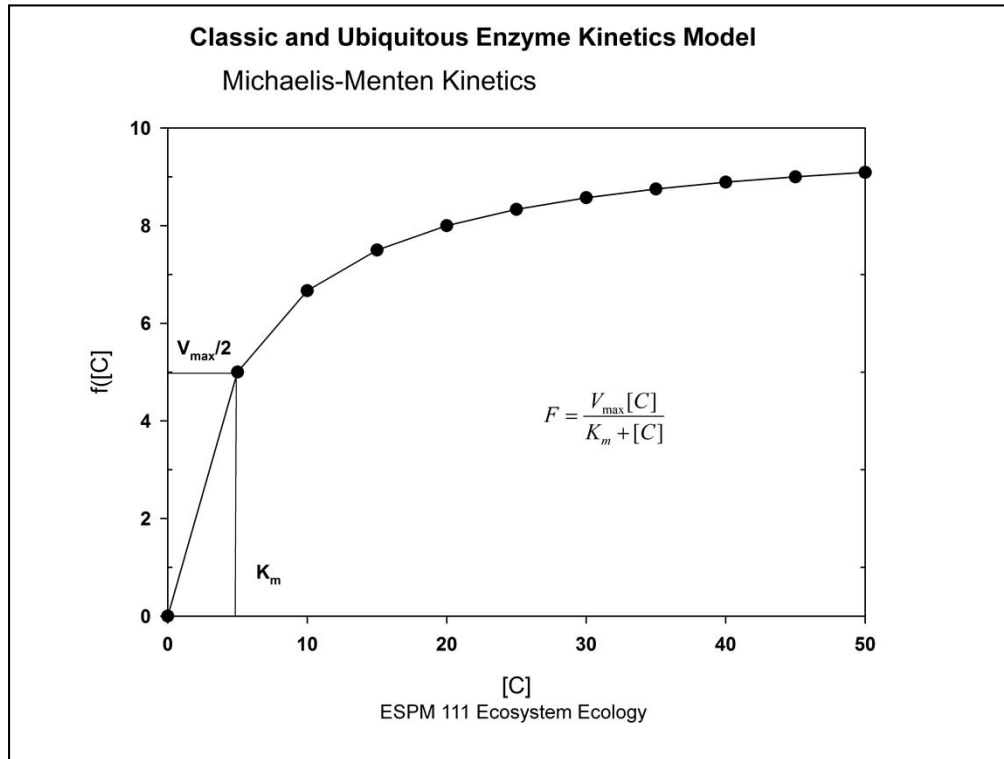
$$R_d \sim \exp(T)$$

Leaf Temperature

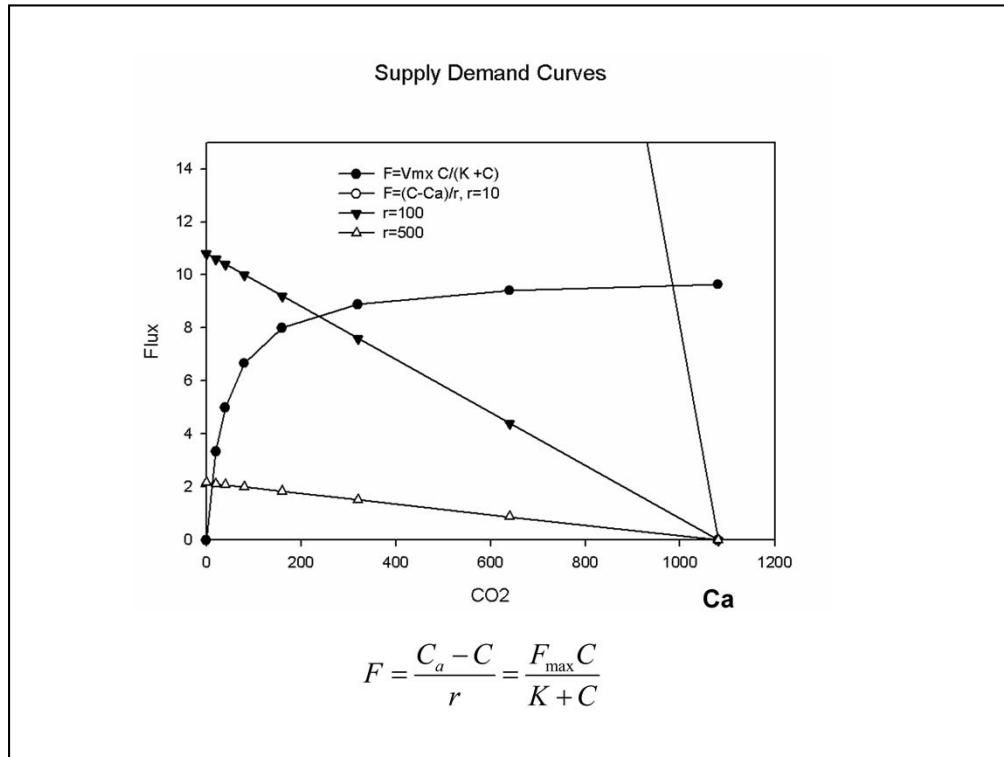
$$L\uparrow \sim T_s^4$$



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Parameters must be fit to use these models. K is the C value at one-half Vmax



In many gas exchange processes there becomes a balance or equilibrium between the supply provided by the diffusion and turbulent transport of a gas from the free atmosphere through the boundary layers and stomata to the site of biochemical consumption in the leaf. In turn the rate of biochemical consumption is a function of the local concentration of C. Ultimately the flux that occurs is at the intersection between the supply and demand curves. If the resistance is nearly zero and the conductance infinite then the intersection occurs at $C_a = C$

Canopy Representation

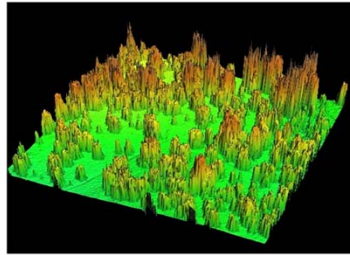


Canopy as a Turbid Medium, with Randomly Distributed Leaves

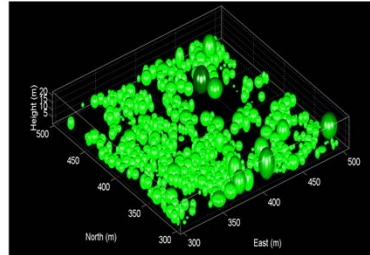
How do we treat a plant canopy? Do we have to know where every leaf and plant is? This can be done. But for practical applications we use statistical models. We assume a canopy is a turbid medium, with randomly distributed leaves, in space, with known leaf inclination angle distributions

Hierarchy of Canopy Radiative Transfer Models

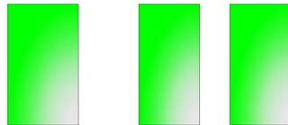
Reality



3-D Representation



2-D Representation



1-D Representation



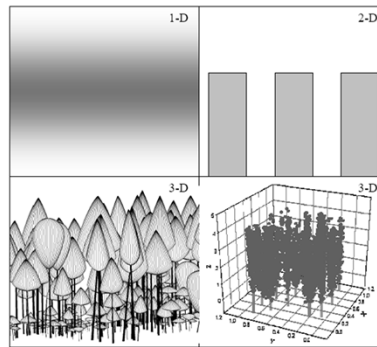
ESPM 228 Adv Topics Biomet and
Micromet

Here are various treatments of light transmission models. The most general is the 1D representation. It works well for closed canopies.

Geometrical Abstraction of the Canopy

- One-Dimensional
 - Big-Leaf
 - Dual Source, Sun-Shade
 - 2-Layer
 - Vegetation and soil
 - Multi-Layered
- Two-Dimensional
 - Dual source
 - sunlit and shaded
 - Vegetated vs Bare Soil
- Three-Dimensional
 - Individual Plants and Trees

Cescatti A. and Ninemes U. - Light harvesting: from leaf to landscape -



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Big-Leaf Vegetation/Bucket Soil

Hierarchy of Ecosystem Models:



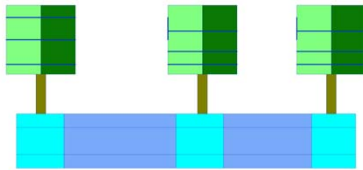
Space:

- Big-Leaf Vegetation/Bucket Soil
- Sun/Shade Vegetation
- Layered Vegetation and Soil

Time:

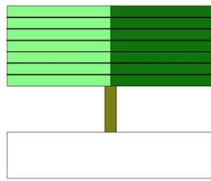
- Hour
- Day
- Month

Multi-layer Vegetation/Soil & Sun/Shade



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CANOAK



Role of Proper Model Abstraction

J.M. Chen et al. / Ecological Modelling 124 (1999) 99–119

117

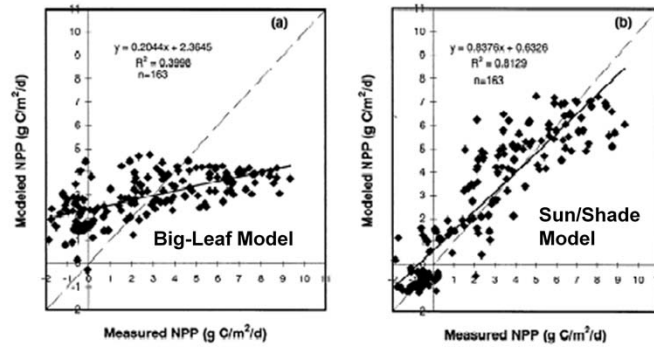
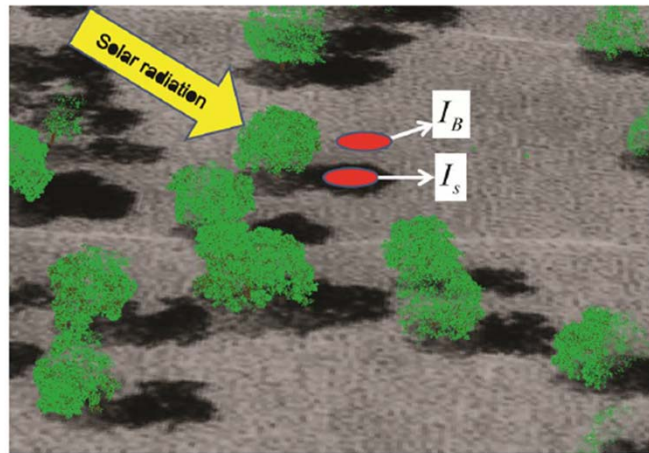


Fig. 9. One-to-one comparison of the measured NPP with the modeled NPP for a mature aspen stand. (a) big-leaf model, and (b) daily integrated model with sunlit-shaded leaf separation.

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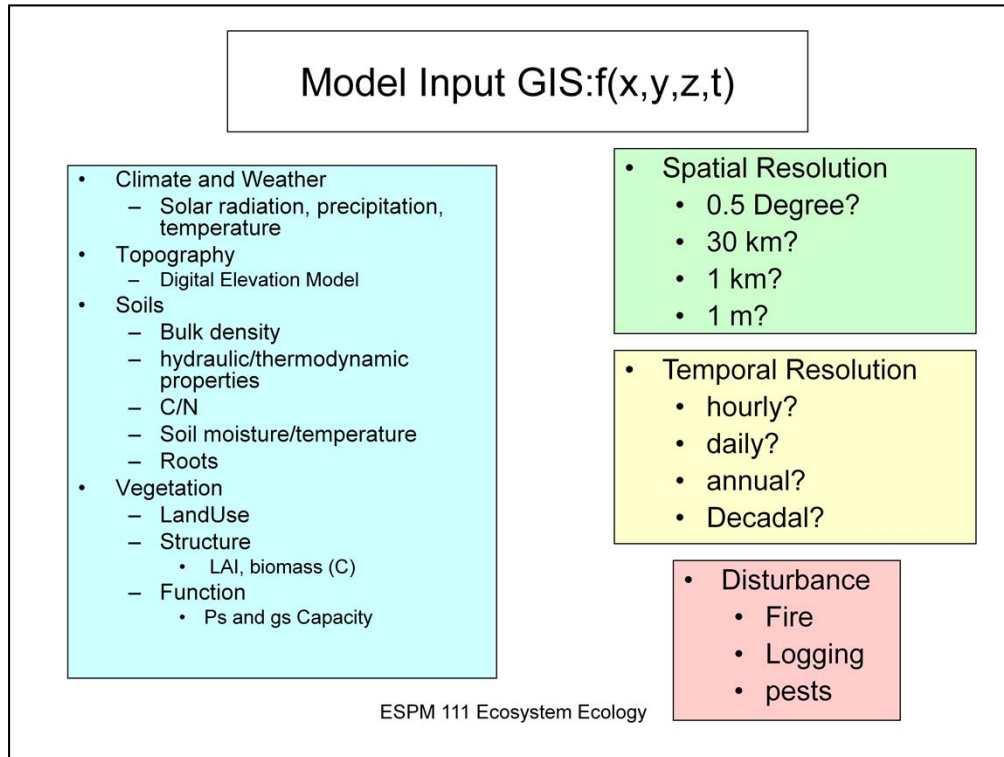
High-Resolution Voxel Based Trees



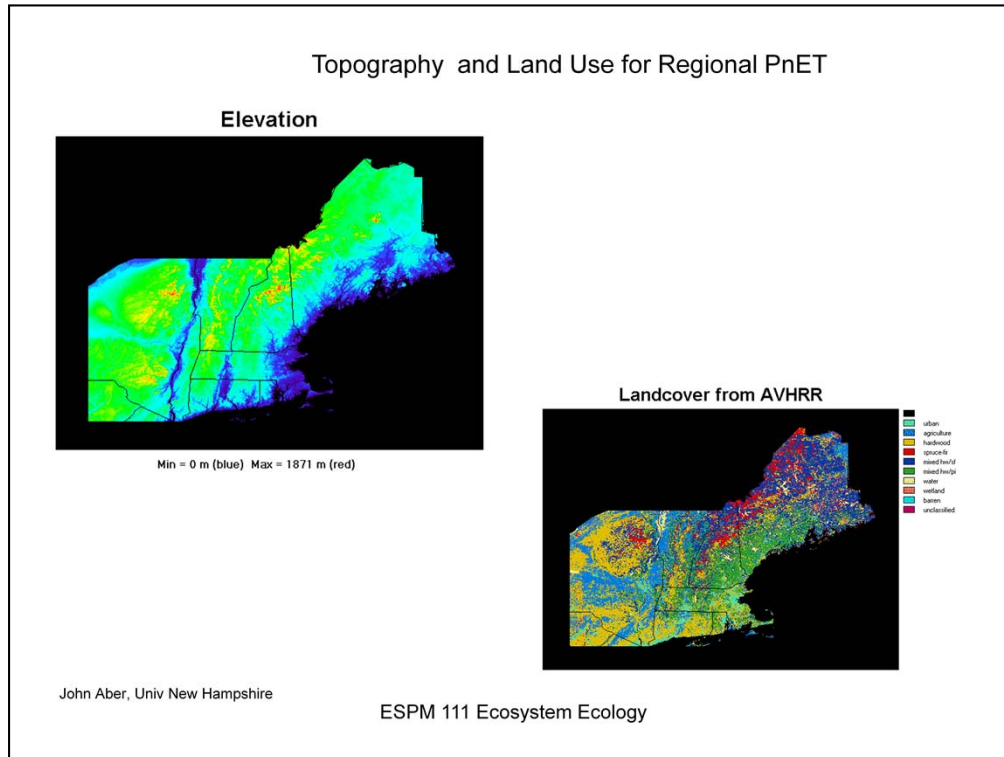
Courtesy of Martin Beland

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With LIDAR we can now measure where every tree is and assess the distribution of foliage using voxels of varying size. As we go to more open canopies it is better to treat the light environment in better detail



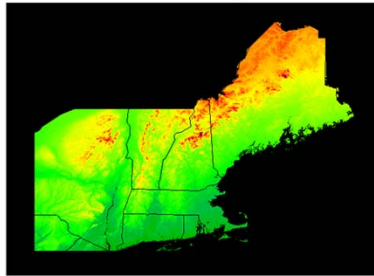
Be careful about representativeness of inputs. Is the temperature at a weather station the same as that of a forest, 10 km away?
What about sub grid spatial variability?



Examples of maps of inputs needed to drive regional ecosystem models

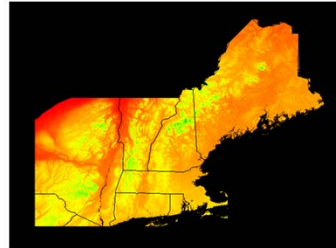
Regional Inputs for Regional Pnet

Mean Annual Temperature



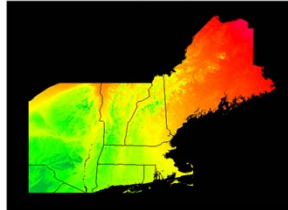
Min = -4.7 deg C (blue) Max = 11.3 deg C (green)

Mean Annual Precipitation



Min = 71 cm (red) Max = 230 cm (green)

Annual Nitrogen Deposition



Min = 3.3 kg N/ha-yr (red) Max = 11.9 kg N/ha-yr (green)

John Aber, Univ New Hampshire

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More variables

New Data Layers on Stand Age and Disturbance History

Y. Pan et al.: Age structure and disturbance legacy of North American forests

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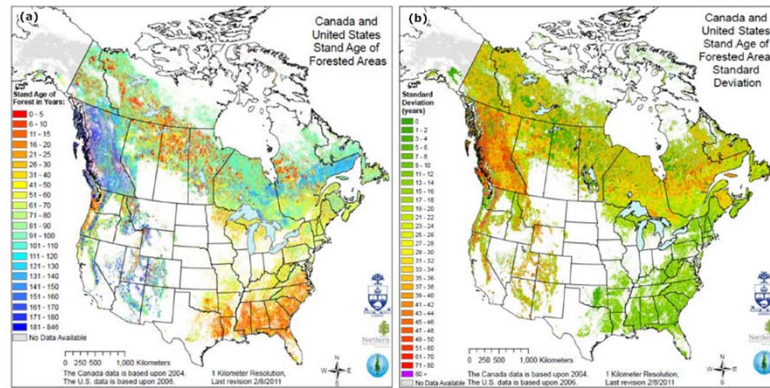


Fig. 1. (a) Forest age distribution in North America (excluding Alaska and Mexico), which was developed by combining forest inventory data (of US and Canada) with several remote sensing based disturbance data sources. (b) The standard deviations of forest ages that characterize uncertainty in the age map (a).

Pan et al 2011 Biogeoscience

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Exciting and new data layer on disturbance

Sources of Geospatial Information for Ecosystem Models

Atlas of the Biosphere Land Use, Climate, etc

<http://www.sage.wisc.edu/atlas/>

International Soil Moisture Network

<https://ismn.geo.tuwien.ac.at/>

Flux Networks, Fluxnet

<http://www.fluxdata.org/default.aspx>

Gridded Climate Data

<http://www.cru.uea.ac.uk/data>

<http://www.esrl.noaa.gov/psd/data/gridded/>

<http://www.prism.oregonstate.edu/>

<http://daymet.ornl.gov/>

NASA Land Products

https://lpdaac.usgs.gov/data_access

Carbon Dioxide Information Center

<http://cdiac.esd.ornl.gov/>

Climate Change in California

<http://cal-adapt.org/>

National Atmospheric Deposition Program

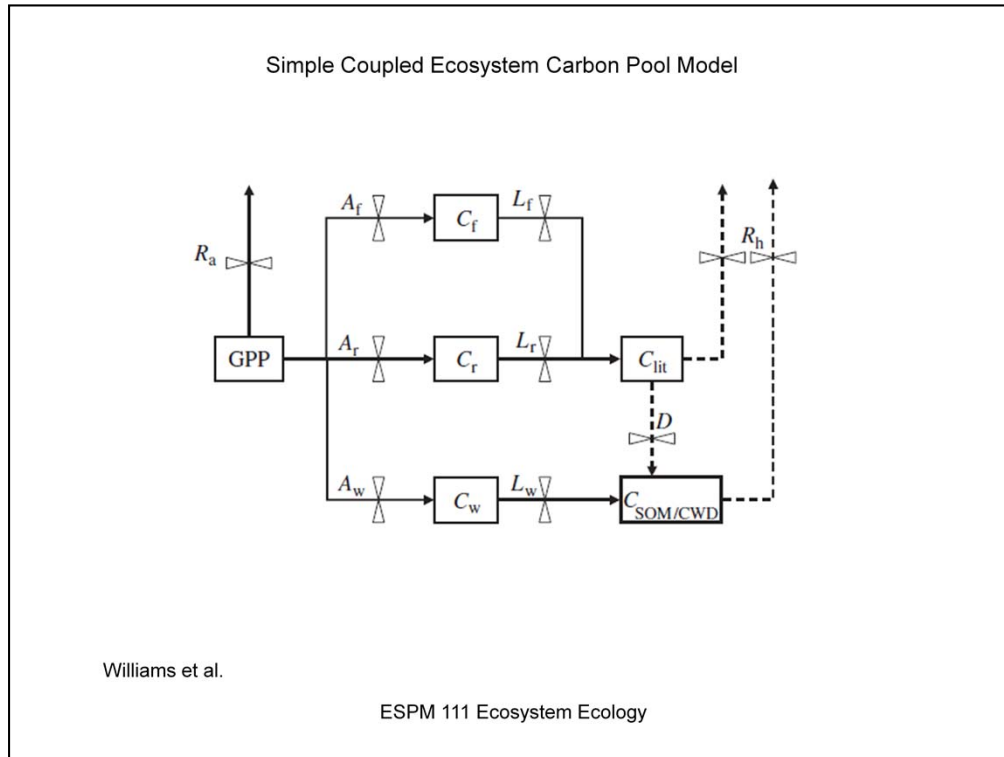
<http://nadp.sws.uiuc.edu/mdn/>

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Ecosystem Models, Examples/Types

- Gap Models
 - Jabowa
 - FORET
 - SORTIE/ED/ED-2
- Biogeochemical
 - Century/DayCent
 - TEM
 - CASA
 - Forest/BIOME-BGC
 - PnET
- Biophysical
 - MAESTRA/CANVEG/CUPID
 - SIB/BATS
 - LSM/CLM
 - SIPNET
- Biogeographical
 - Miami
 - DOLY
 - MAPSS
 - BIOME
- Dynamic Global Vegetation Models
 - Hybrid
 - Lund-Potsdam-Jena (LPJ)
 - IBIS
- Next Generation Land-Climate Models
 - JULES
 - ORCHIDEE
 - CASA-CLM
 - JSBACH

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Very simple 4 pool carbon model. Considers the gains and losses of Carbon by photosynthesis, GPP, how photosynthesis (A) is partitioned into the foliage, root and wood fractions, how these pools (C) change as there are respiratory losses. Then litter either is lost by respiration or turned into soil detritus, which respire, too.

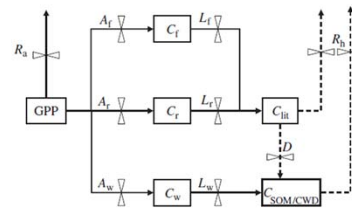
Simple Set of Coupled Differential Equations to Solve the problem

$$V_a \rho_a \frac{dC_a}{dt} = -P_{plant} + R_{plant} + R_{soil}$$

$$V_{plant} \frac{dC_{plant}}{dt} = P_{plant} - R_{plant} - F_{litter}$$

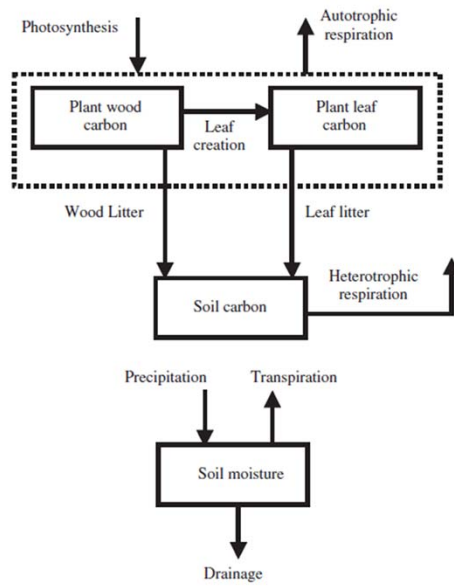
$$V_{litter} \frac{dC_{litter}}{dt} = F_{litter} - R_{litter}$$

$$V_{soil} \frac{dC_{soil}}{dt} = F_{litter} - R_{litter} - R_{soil}$$



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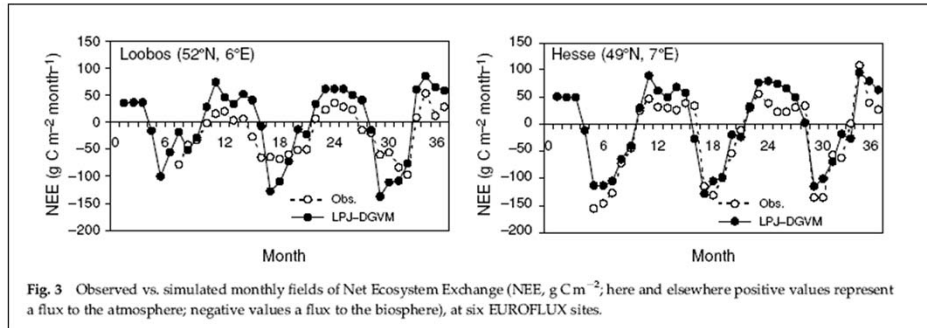
Closure is important. We need the same number of equations as unknowns. And we need to define model parameters



Braswell et al

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Model Validation How Good is Good Enough?



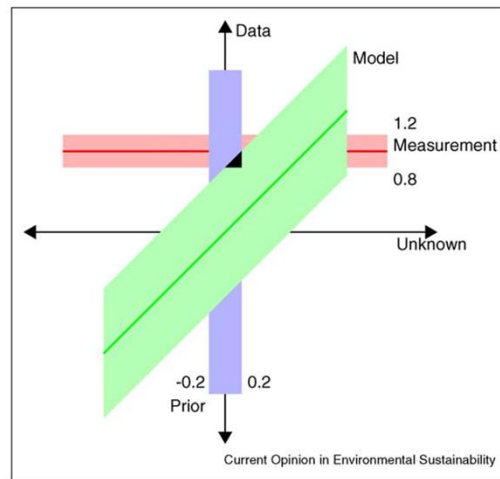
Sitch et al. 2003 GCB

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How good is good enough

Model Data Fusion Why Data or Models May be Correct, or Incorrect

Figure 1

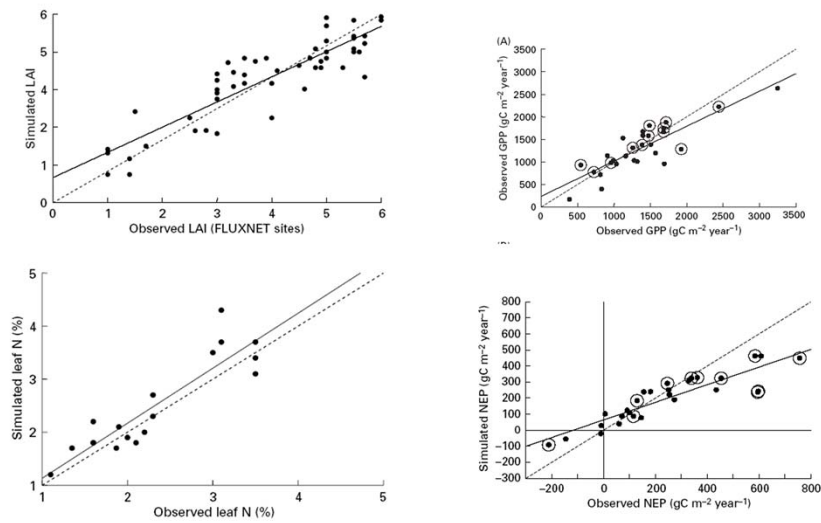


There are imperfections
In model, parameters,
And measurements

The Black Triangle is the
Intersection of data, model
And measurements

Rayner 2010 Current Opinions in Environment Sustainability
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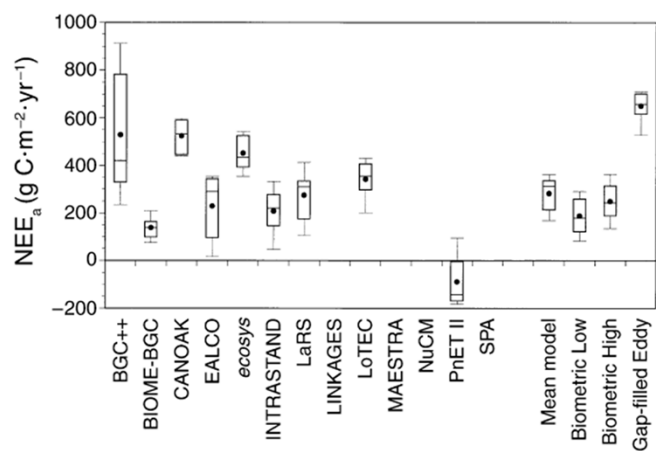
How Good is Good Enough, part 2



Woodward and Lomas, 2004

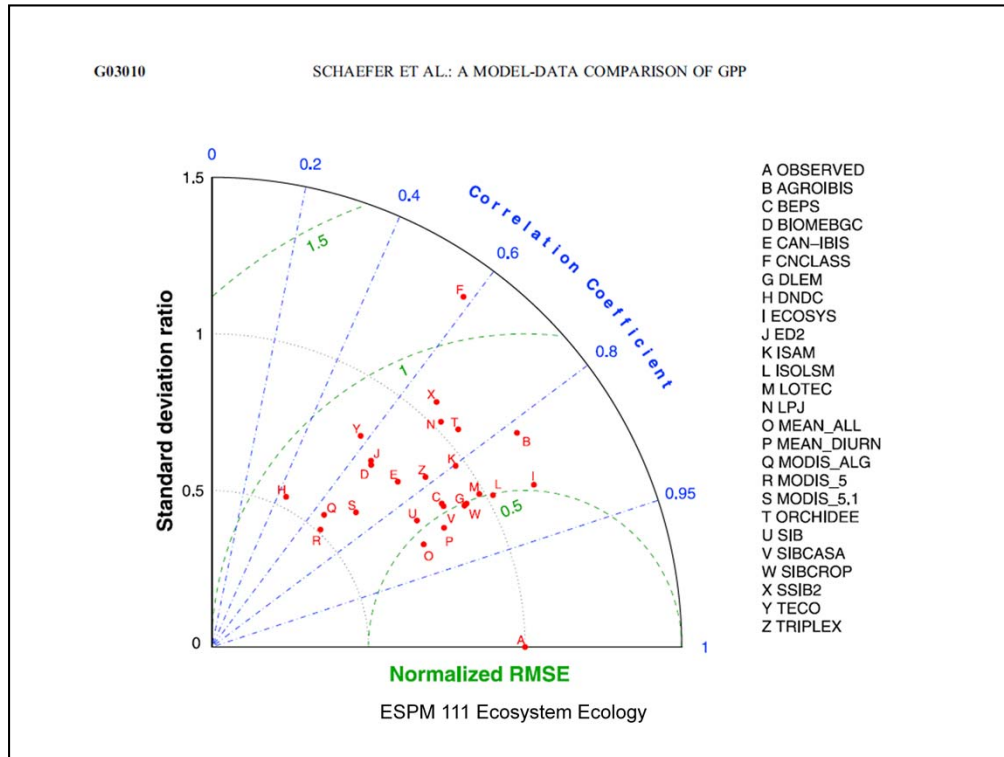
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Model Validation: Who is Right and Wrong, and Why?



Hansen et al, 2004 Ecol Monograph
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Test of Models at Walker Branch, a deciduous forest



Ways to test groups of models with data from flux networks, using lots of data and lots of models. Here it looks like most of the 'best' models are not doing well when tested with data.

Role of Time Scale when Validating Models

1200 M. B. SIQUEIRA *et al.*

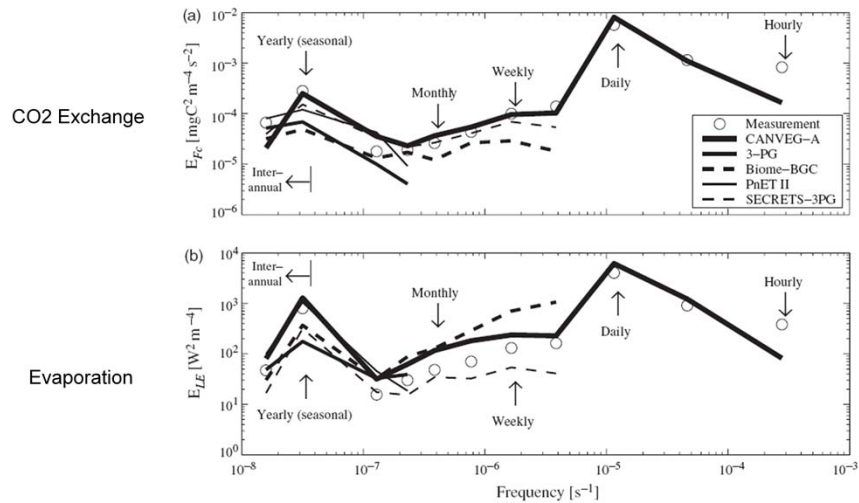


Fig. 4 Measured and modeled power spectra for the CO₂ flux F_c [panel (a)] and latent heat flux LE [panel (b)].

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The time scale at which you test a model is important too. Some models may get short term fluxes wrong, and long integrations right, due to offsetting errors.

Same Model, but Different Parameters: Role of Monte Carlo Model parameterization

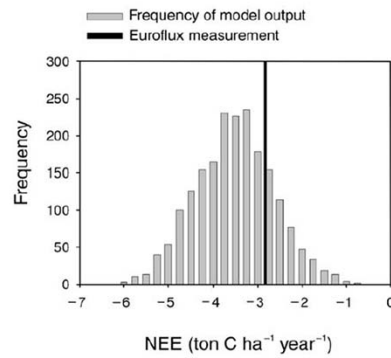


Figure 2. Distribution of the total net ecosystem exchange (NEE; Mg C ha⁻¹ year⁻¹) in 1997 for the Hesse forest in France. The calculation of this distribution is based on 2000 Monte Carlo simulations. Only the uncertainty of ten key parameters was taken into account. The black bar above shows the measured (Euroflux) NEE value and does

Verbeek et al 2006 Tree Physiol

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Models have many uncertainties and it is important to quantify this uncertainty

Will Be?



- Even Better Coupled Biophysical-Biogeochemical-Ecosystem Dynamics Models [e.g. LPJ (Prentice et al.); IBIS, (Foley et al.); ORCHIDEE; CASA/CLM]
- Predict Functional type, LAI, Structure, phenology, soil moisture + Ecosystem responses to CO₂, T, ppt + N perturbations and disturbance
- Improved Coupling of Biogeochemistry to Climate Models
- Better Spatial Inputs of Climate and Plant Drivers
 - Lidar Mapping of Forests and Vegetation
- Better Model Parameterization
- Fire Probabilities
- Better Phenology
- Better Allocation
- Better Disturbance Maps

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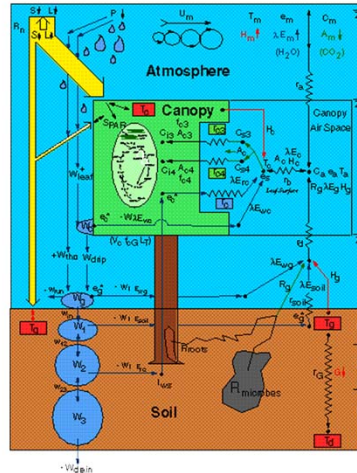
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Big-Leaf Model

SiB2 *Simple Biosphere Model* Version 2

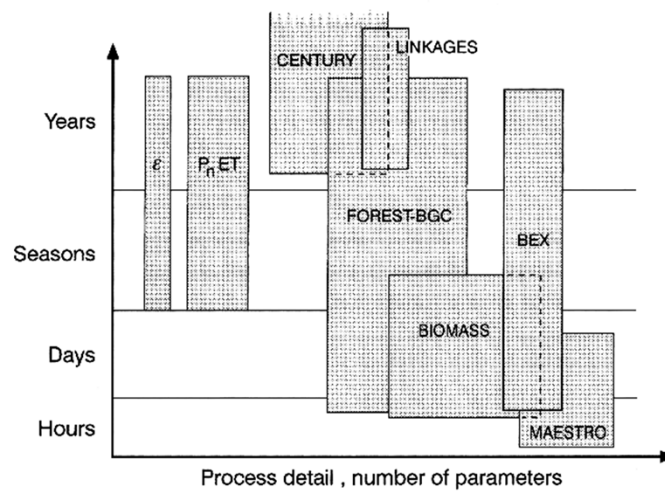
Ohm's Law Analog for Fluxes

$$F = \frac{V}{\Sigma R}$$



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SVAT MODEL COMPLEXITY



Landsberg and Gower, 1997

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First Global Ecosystem Model Miami Model, Helmut Lieth

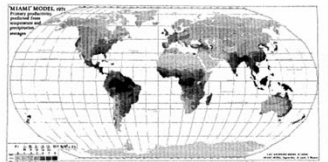
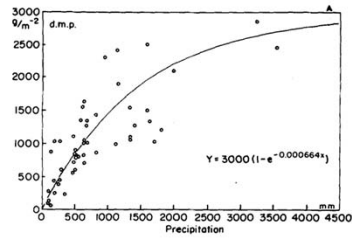
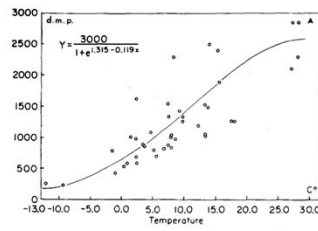


Fig. 4. "Miami evapotranspiration map" - this map gives predictions of the potential evapotranspiration and precipitation as related to the annual temperature and precipitation. The predictions are based on the two equations shown in Fig. 1 and 2 and temperature and precipitation values from Walter and Lieth (1963/1967).

Lieth, 1973, Human Ecology

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Jabowa/FORET

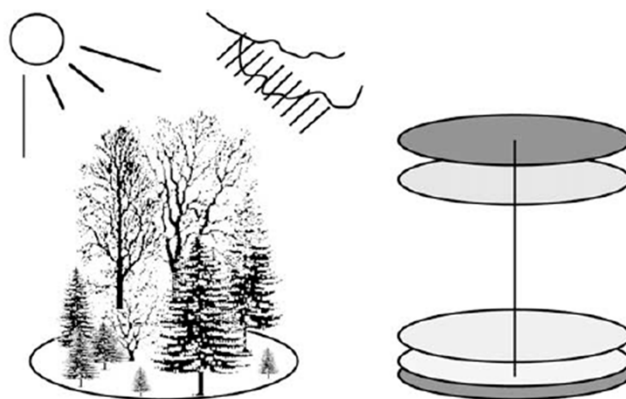
The Grand-Daddy of Ecosystem Gap
Dynamic Models



- Abstraction
 - Forest is abstracted as composite patches and gaps
 - Patches are horizontally homogeneous
 - ~100 m²
 - Leaves in a thin disk at top of tree
 - No interaction among patches
 - Individual Based
- Growth
 - Competition for Light and Resources (soil moisture, Temperature, N)
- Mortality
 - Stochastic
- Establishment and Recruitment
 - Stochastic
 - All seeds available
 - Ample water for establishment

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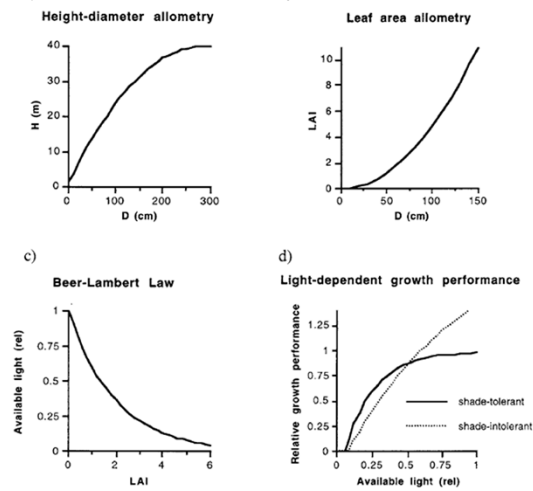
Gap Models, JABOWA, etc



Bugmann, Climatic Change, 2001

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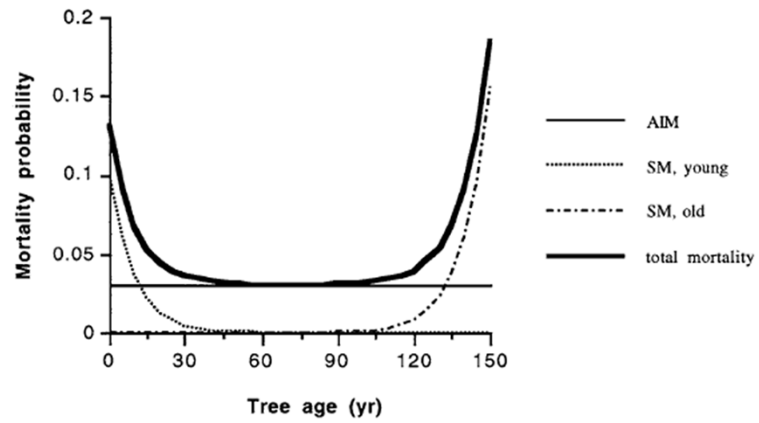
Conceptual Forcing Functions by Species



Highly Parameterized!

Bugmann, 2001 Climatic Change ESPM 111 Ecosystem Ecology

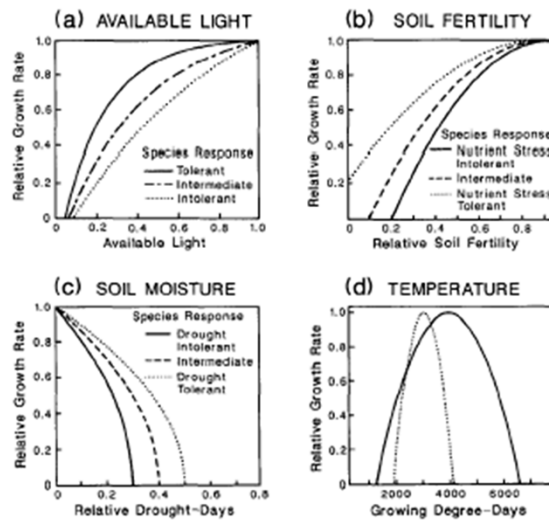
Mortality Functions



Bugmann, 2001 Climatic Change

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Conceptual Forcing Functions, part 2



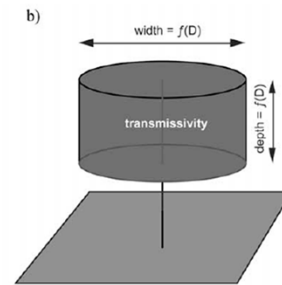
Shugart et al, 1992 Ann Rev Ecol

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SORTIE



- Follows fate of individual trees
- Four submodels
 - Resource Limitations (light, water, N)
 - Growth = $f(\text{species, diameter and light index})$
 - Mortality = $f(\text{species, carbon balance})$
 - Recruitment (number, size seeds, germination, survival, root sprouting)
- Parameterization
 - Field data
 - Regression equations
 - Maximum Likelihood

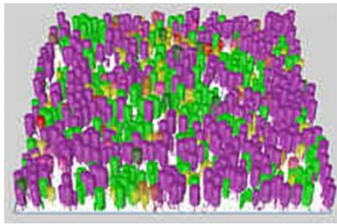


Pacala 1996 Ecol Monograph

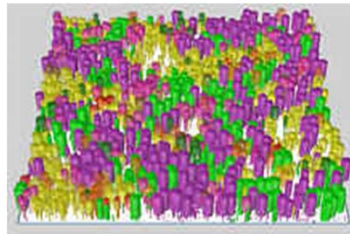
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Spatial Representation of Trees in SORTIE

Undisturbed, 500 years



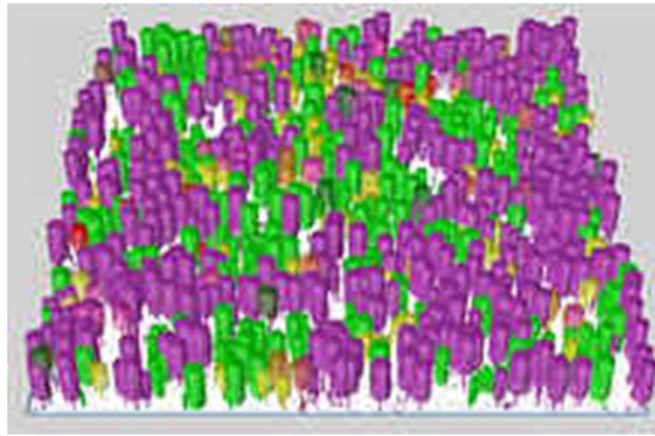
Disturbed, 500 years



Pacala 1996 Ecol Monograph; Deutschman et al 1997 Science

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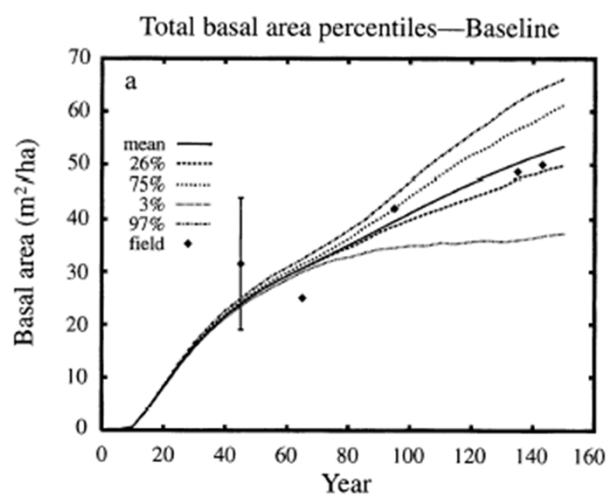
<http://www.sciencemag.org/feature/data/deutschman/index.htm>



[Open MPEG HyperLink](#)

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Testing SORTIE



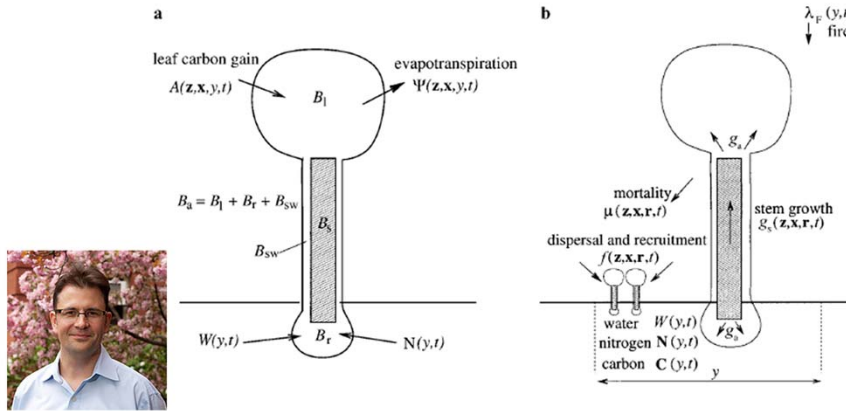
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Ecosystem Dynamic Model, ED SORTIE with EcoPhysiology

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P. R. MOORCROFT ET AL.

Ecological Monographs
Vol. 71, No. 4

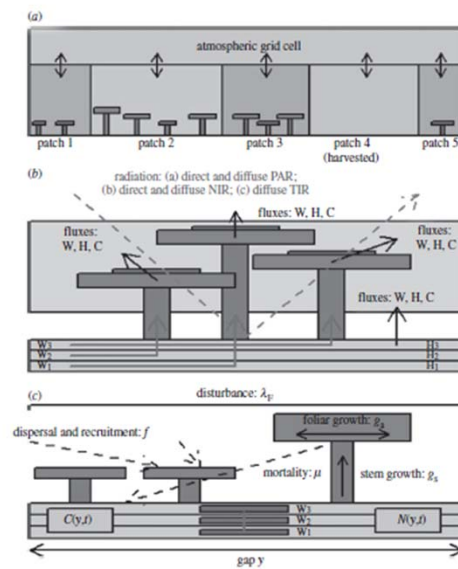


Moorcroft et al 2001, Ecol Monograph

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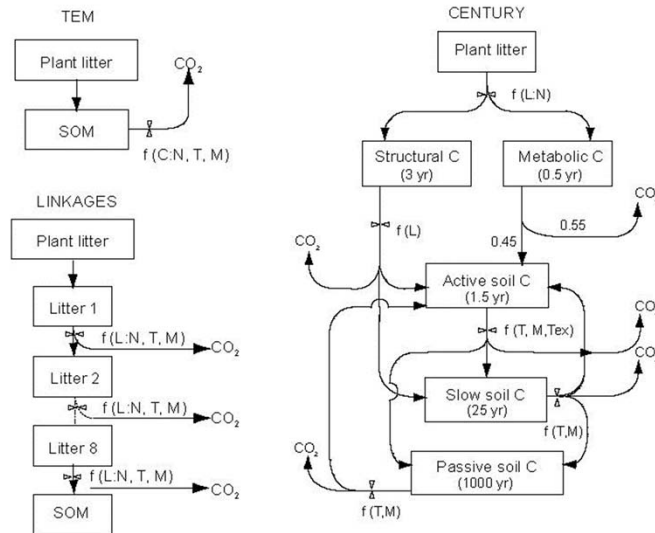
ED-2

Predicting regional ecosystem dynamics D. Medvigy & P. R. Moorcroft



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Multi-Pooled Biogeochemical Cycling Models

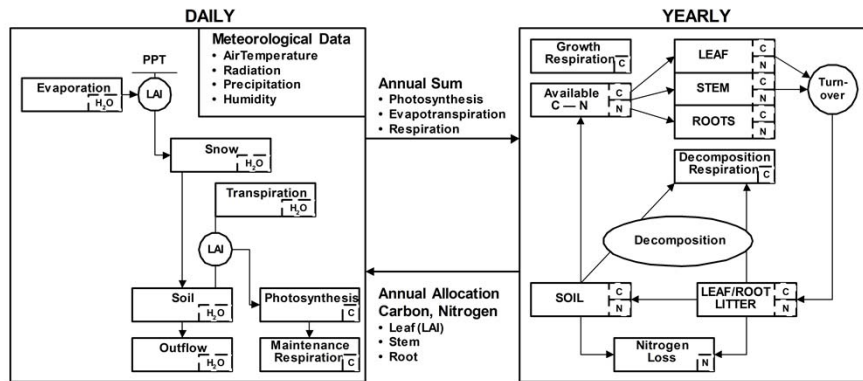


Chapin et al.

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Biogeochemical Cycling Model at Daily and Annual Time Steps

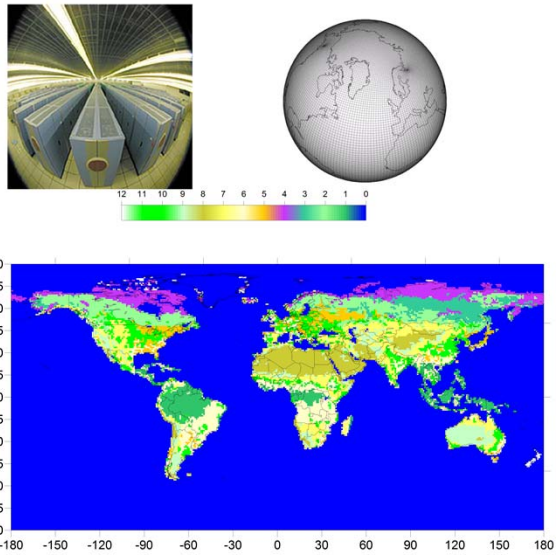
Forest — BGC



Coughlan and Running, 1988

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Dynamic Vegetation-Climate Computer Models



deFries Global 1x1 degree land cover map

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Coupled Climate-CASA, Contemporary Global Biogeochemical Cycling Model

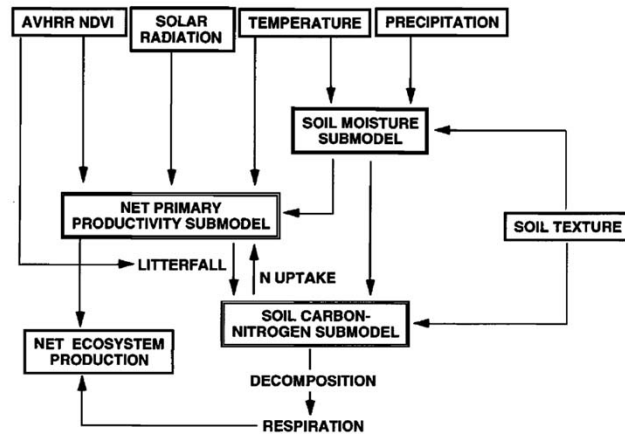
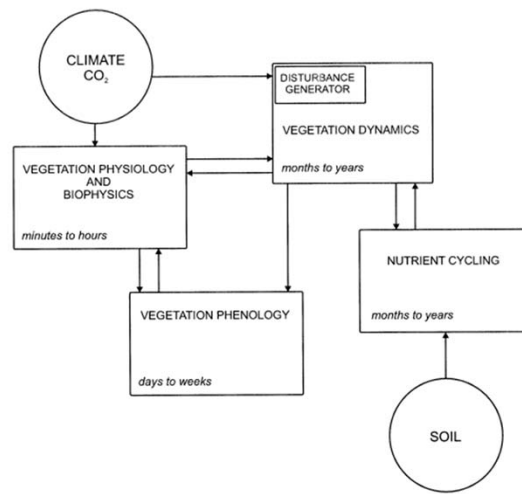


Fig. 1. Model integration framework. Global climate data sets are combined with soil texture settings to compute the monthly water balance, which controls NPP and soil microbial activity.

Dynamic Global Vegetation Model

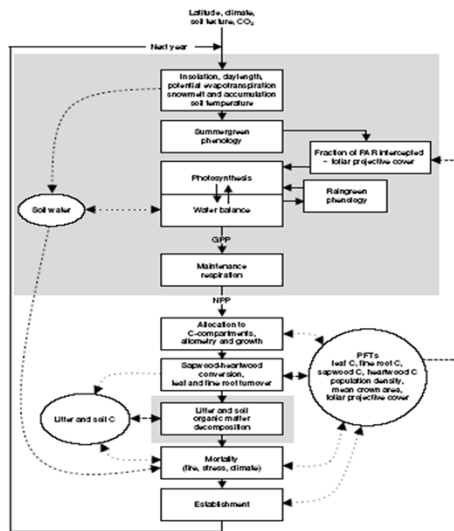


Cramer et al 2001, GCB

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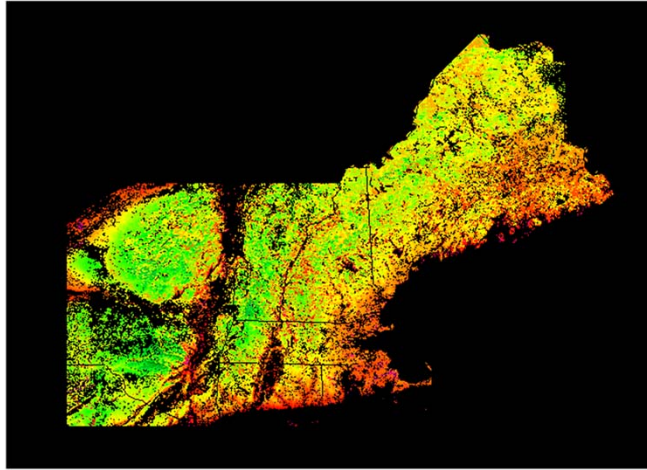
LPJ Global Dynamic Vegetation Model

164 S. SITCH *et al.*



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Annual Net Ecosystem Production



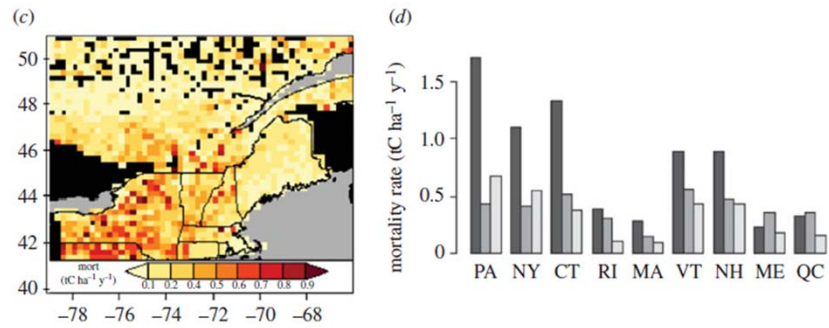
Min = -271 g C/m2-yr (black) Max = 345 g C/m2-yr (green)

<http://www.pnet.sr.unh.edu/subpages/graphics/bkg8.gif>

PnET

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Computing Mortality Maps with Optimized ED-2 Model



Medvigy and Moorcroft, 2012 Phil Trans Royal Soc B

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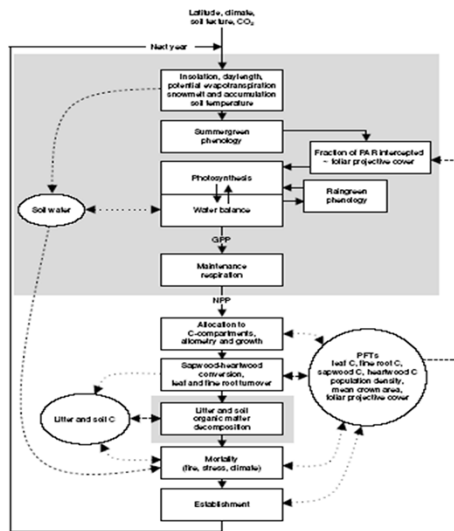
More on data assimilation

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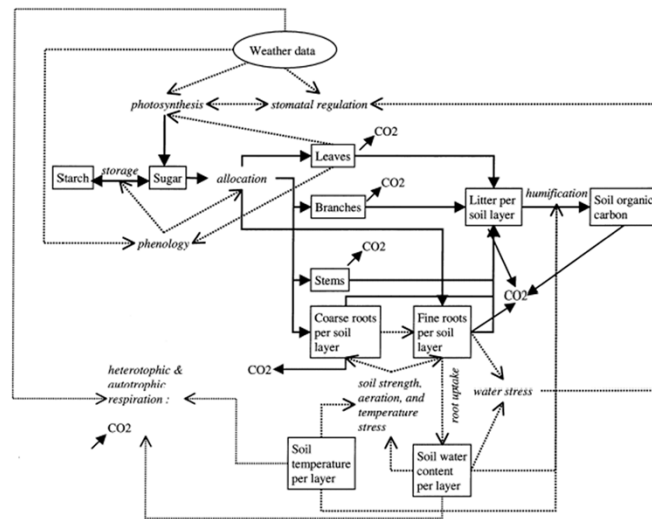
LPJ Global Dynamic Vegetation Model

164 S. SITCH *et al.*



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ASPECTS: Coupled Forest Ecosystem Model
Rasse et al, Ecol Modeling



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Ecosystem Models, Examples

- Gap Models
 - Jabowa
 - FORET
 - SORTIE
 - ED
- Biogeochemical
 - Century
 - TEM
 - CASA
 - Forest/BIOME-BGC
 - PnET
- Biophysical
 - SIB
 - BATS
 - LSM
 - Canveg
 - SPA
- Biogeographical
 - Miami
 - DOLY
 - MAPSS
 - BIOME
- Dynamic Global Vegetation Models
 - Hybrid
 - Lund-Potsdam-Jena (LPJ)
 - IBIS



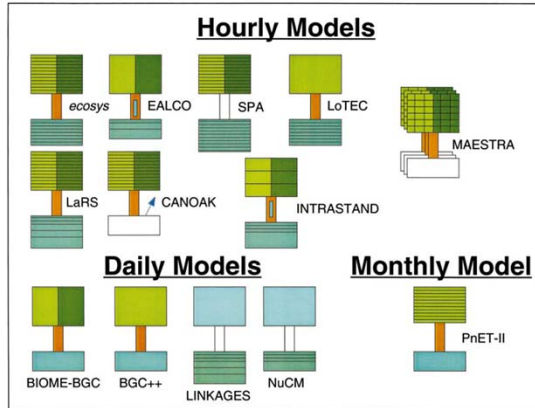
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Hierarchy of Models:

August 2004

CARBON AND WATER MODEL EVALUATIONS

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Space:

Big-Leaf Vegetation
Bucket Soil

Sun/Shade Vegetation

Layered Vegetation and Soil

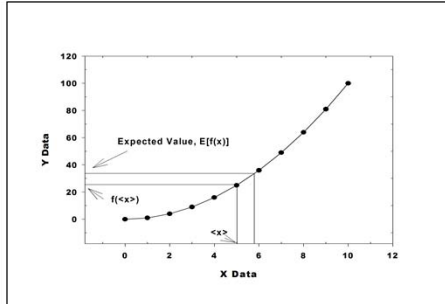
Time:

Hour
Day
Month

After Hanson et al Ecol Appl 2004

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Why Non-linearity is Important?



Jensen's Inequality

$$f(\langle x \rangle) \neq \langle f(x) \rangle$$

Taylor's Series Expansion

$$E[f(x)] = f(\bar{x}) + \frac{1}{2} \frac{\partial^2 f(\bar{x})}{\partial x^2} \sigma(\bar{x})^2$$

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