

THE CONTROVERSY OVER LIVING FORCE: LEIBNIZ TO D'ALEMBERT

A thesis submitted to the Graduate School of  
the University of Wisconsin in partial fulfillment  
of the requirements for the degree of Doctor of  
Philosophy.

by

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Degree to be awarded

January 19—

June 19<sup>67</sup>

August 19—

To Professors: Hebert ✓

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This thesis having been approved in respect  
to form and mechanical execution is referred to  
you for judgment upon its substantial merit.

Robert M. Bock

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Approved as satisfying in substance the  
doctoral thesis requirement of the University of  
Wisconsin.

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Date of Examination, March 22, 1967

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LEIBNIZ TO D'ALEMBERT

BY

CAROLYN ILTIS

A thesis submitted in partial fulfillment of the  
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DOCTOR OF PHILOSOPHY

(History of Science)

at the

UNIVERSITY OF WISCONSIN

1967

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#### ACKNOWLEDGMENTS

It is a pleasure to record my gratitude to Professor Erwin N. Hiebert who supervised the writing of this dissertation. His many very valuable suggestions, his patience and thoroughness have made this study exciting and its completion possible. I am also deeply indebted to Professor Julius Weinberg for his criticisms and suggestions regarding the philosophical aspects of this dissertation, to Professor Keith Symon for his comments on aspects of Leibniz's physics and to Dr. Joan Bromberg for her critical reading and sustained encouragement. Thanks and acknowledgement are extended to the E. B. Fred Fellowship Committee and the Carnegie Corporation of New York who provided the funds supporting the research.

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